

Local search framework for irregular shaped stock- cutting

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Aims and motivation

Develop an understanding of how well various problem specific decisions work in a local search framework for the irregular cutting problem.

- Investigate the performance of various local search neighbourhoods for irregular stock- cutting
- Use iterated local search to minimise parameter refinement
- Remove all problem specific enhancements
- Not to beat the best but to learn more about the relationship between local search and such problems

Aims and motivation

Most of the successful implementations in the literature employ problem specific enhancements and/or complex optimisation procedures

- Single or multiple (conflicting) objectives
- Different representations of the solution
- Computationally expensive enhancements
- Complex neighbourhood move criteria

Why they work is often conjecture

This study

Constructive algorithms have been shown to be an effective solution approach.

However, decoding the representation as a permutation of pieces and the layout of the solution is not a 1-1 mapping

Hypothesis: There exists significant redundancy in the search algorithm as a result of reproducing the same solution from a different representation

Iterated local search

1. randomly generate initial solution (S_0) with cost $C(S_0)$
let $S_{\text{best}} = S_0$
 2. If termination conditions are satisfied STOP
 3. Let $S_i \in N(S_0)$ $i=1, n$
for all i if $C(S_i) < C(S_0)$ accept $S_0 = S_i$
if $C(S_0) < C(S_{\text{best}})$ $S_{\text{best}} = S_0$
return to 2
 4. if $i=n$ perform kick $S_0 = S_k$
return 2
- END

Iterated local search and iteratively construct solution

- solution represented by permutation of pieces
- initial solution randomly generated
- neighbourhood of piece j all possible insert moves
- piece j selected without replacement
- solution constructed using a outer-left strategy
- cost = length of constructed layout
- kick = K random insert or swap move

Investigation of data with construction algorithm

Step 1 : record searched neighbourhood moves (piece m inserted in location j) where $C(S_i) = C(S_0)$

Step 2 : identify distance moved in permutation
($\text{abs}(\text{pos}(m) - j)$)

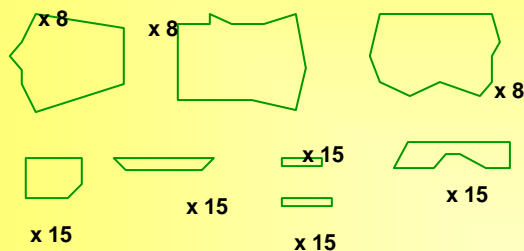
Step 3 : identify no. of changed co-ordinate positions of placed pieces in solution layout

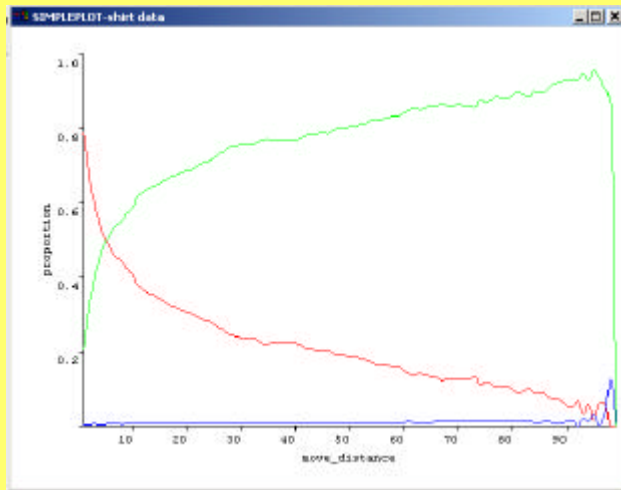
Step 4 : identify piece type of m for each identified move

Data set:

Shirt patterns, Dowsland et al (1998)

99 pieces, stock sheet width = 40

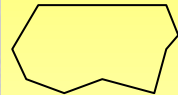
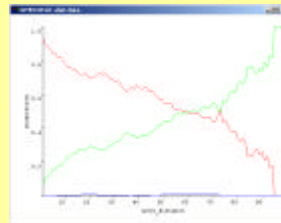
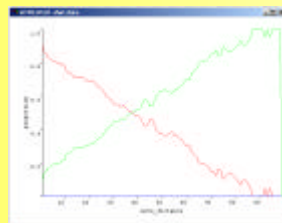
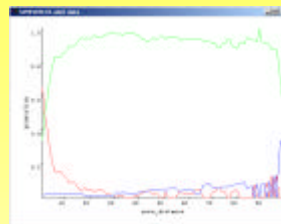
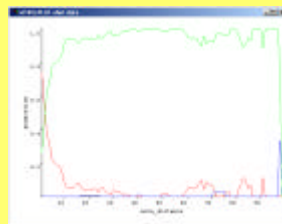
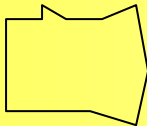




$\Delta \text{ cost} = 0$

$\Delta \text{ cost} < 0$

$\Delta \text{ cost} > 0$

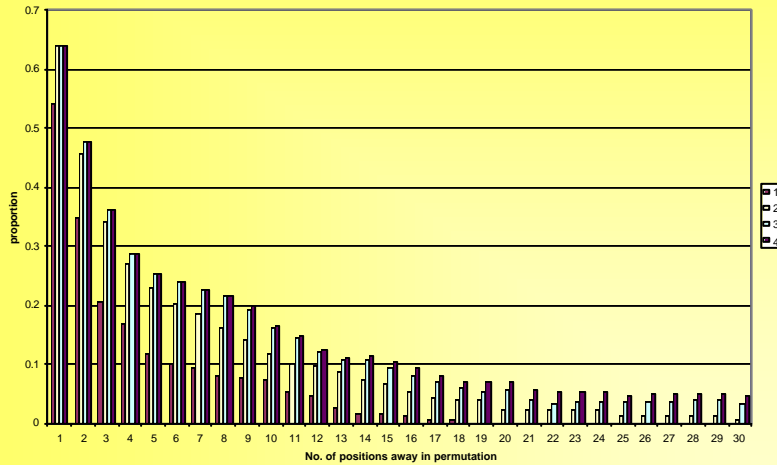


$\Delta \text{ cost} = 0$

$\Delta \text{ cost} < 0$

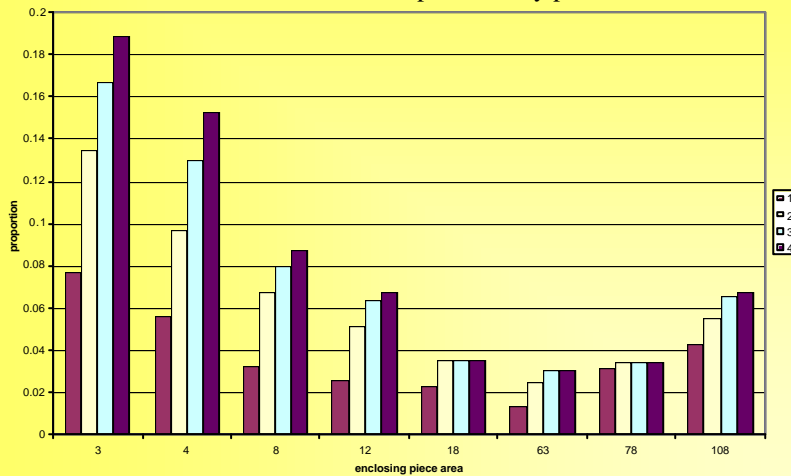
$\Delta \text{ cost} > 0$

No. of different co-ordinate positions by move distance



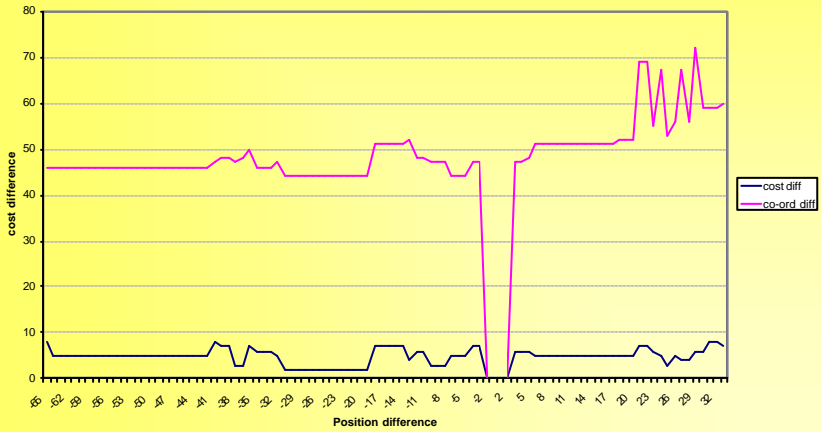
Over all piece types

No. of different co-ordinate positions by piece area

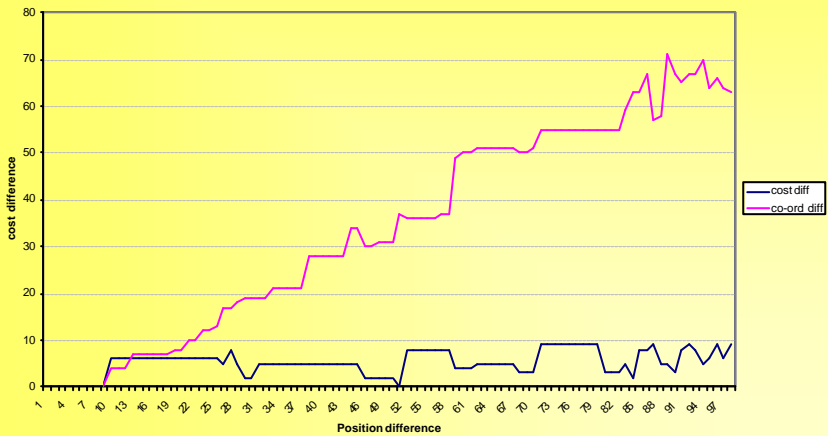


Over all distances in permutation

Shirt - peice type 2

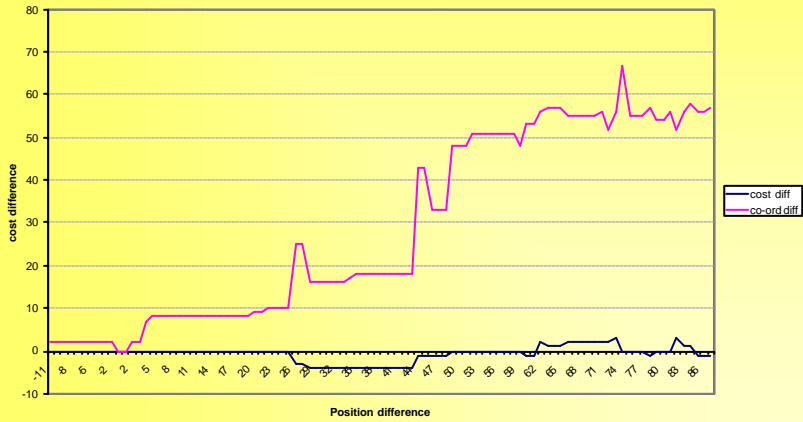


Shirt - peice type 3

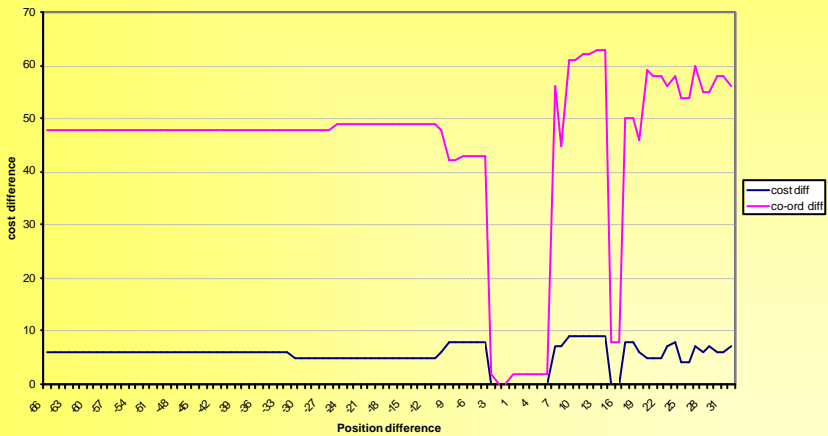




Shirt - peice type 5



Shirt - peice type 7



Summary

- Construction algorithms are successful but slow
- There is no 1-1 mapping between the solution representation and the physical solution
- Short cuts need to be made to establish local optima and make a broad search of the neighbourhood
- There exist systematic interactions between the data and the search neighbourhood
- These, if discovered, can be exploited to reduce redundancy