Micromagnetic Modelling of the Dynamics of Exchange Springs in Multi-Layer Systems

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Exchange springs are formed in multilayers of alternating hard and soft ferromagnetic materials which are exchange coupled at their interfaces. These systems are rich of interesting physical properties, which can be tuned by selecting suitable geometries and compositions. In this paper, we present a computational study of the dynamics of a tri-layer DyFe₂/YFe₂/DyFe₂ exchange spring system near the bending field (the field required to twist the magnetization of the soft YFe₂ layer out of the aligned state). The dynamical reaction of the system to small variations of the applied field is studied and its oscillatory nature is analyzed numerically. The behaviors of the decay times, the frequencies, and amplitudes reveal enhanced responses of the system near the bending field.

Index Terms—Dysprosium alloys, exchange springs, finite-element method, magnetic layered films, magnetic multilayers, micromagnetism, Nimag, numerical analysis, yttrium alloys.

I. INTRODUCTION

Exchange spring systems are composites of magnetically hard and soft materials that are exchange coupled across their interfaces. They are promising candidates for many technological applications. They could be used to obtain high densities in storage media, while keeping acceptable writability and thermal stability [1]. They could also be used as high-performance permanent magnets [2] or as giant magneto-resistance (GMR) sensors. An important feature of these systems appears when a suitable external field is applied: the magnetization of the soft material responds in a position dependent way, being bounded to the magnetization of the hard material near the interfaces and twisting towards the applied field in the bulk. This resembles a mechanical torsion spring, thus comes the name “exchange spring.” The torsion is exhibited only when the applied field exceeds a particular value called the bending field. For lower values the fully aligned state is preferred, because it turns out to minimize the energy, as shown by simple theoretical models [3]. The slope of the magnetization (with respect to varying the applied field) is large close to the bending field. This may be of technological relevance as a small applied field results in a large change in magnetization. Moreover, Brillouin light scattering experiments have shown interesting properties near the bending field, where the measured magnon frequency reaches a minimum value [4].

In this paper, we study the dynamics of a model of a hard–soft–hard exchange spring system in the vicinity of the bending field. We have chosen material parameters similar to a DyFe₂/YFe₂/DyFe₂ sample, which has been the subject of experimental investigation in our group.

II. MODEL

The system is a thin film made of one central magnetically soft YFe₂ layer sandwiched between two thinner magnetically hard DyFe₂ layers [see Fig. 1(a)]. Three different kinds of atoms are present in this system: one rare earth metal (Dy) and two transition metals (Fe and Y). The yttrium has negligible magnetic moment: only the iron moments contribute to the magnetization of the central layer. Conversely, in the two external layers both the atomic species of the DyFe₂ compound give a relevant contribution to the magnetization. For the temperature considered here (100 K), the magnetic moment of iron is weaker than the one of dysprosium and is forced to be antiparallel to it by the strong antiferromagnetic coupling, which makes the DyFe₂ a ferromagnet. Moreover, Dy experiences a strong magnetocrystalline cubic anisotropy which makes the two external layers magnetically hard. The Fe–Fe exchange coupling is even stronger than the Dy–Fe coupling [5] and opposes to the spatial variation in the orientation of the magnetizations. The coupling occurs also across the boundary surfaces between the layers. This is what allows the system to develop exchange spring configurations, keeping the iron moments bounded to the dysprosium moments of the hard layers at the boundaries. The effects of strain on the magnetic anisotropy of MBE-grown DyFe₂/YFe₂ superlattices are negligible at temperatures below ~100 K [6].

We study the system with a unidimensional model along the out-of-plane direction, neglecting spatial variations of the magnetization across the plane of the layers. The configuration of the magnetic moments in the system is represented by two continuous magnetization fields \( M_{Dy}(z) \) and \( M_{Fe}(z) \) defined over the 1-D space: \( M_{Dy} \) is the moment density of Dy atoms in DyFe₂
and $M_{Fe}$ is the moment density of Fe atoms in DyFe$_2$ and YFe$_2$. Their norms are $M_{Dy} = ||M_{Dy}||$ and $M_{Fe} = ||M_{Fe}||$, which at the temperature of 100 K are $M_{Dy} = 1.73 \times 10^6$ A/m and, for both DyFe$_2$ and YFe$_2$, $M_{Fe} = 0.55 \times 10^6$ A/m. The Brown’s theory of micromagnetics is used to derive the effective fields acting on $M_{Dy}$ and $M_{Fe}$:

$$H_{Dy} = H_{app} + H_d + H_{anis} + (J/\mu_0)M_{Fe}$$
$$H_{Fe} = H_{app} + H_d + H_{exch} + (J/\mu_0)M_{Dy}.$$ 

The applied field acts on both dysprosium and iron. $H_{Dy}$ also receives a cubic anisotropy contribution, whose three axes are shown in Fig. 1(a). The three coefficients used in the anisotropy expansion [7] are $K_1 = 33.9 \times 10^6$ J/m$^3$, $K_2 = -16.2 \times 10^6$ J/m$^3$, and $K_3 = 16.4 \times 10^6$ J/m$^3$. The iron experiences an exchange field $H_{exch} = (2A/\mu_0M_{Fe})V^{3/2}m_{R}$, where $A = 1.46 \times 10^{-11}$ J/m is the exchange coupling constant, $\mu_0$ is the free space permeability, and $m_{R} = M_{R}/M_{Fe}$. The dipolar field $H_d$ is calculated as $H_d = -M_d z$, where $M_d$ is the out-of-plane component of the total magnetization field and $z$ is the unit vector which points towards the positive $z$ direction. This contribution evidently tries to reduce the surface magnetic charges, pulling the magnetization into the plane of the film. The Dy–Fe coupling is modeled by an extra energy term $U = J \int M_{Dy} \cdot M_{Fe} dz$ in the Hamiltonian, where $J = 2 \times 10^{-4}$ N/A$^2$ is the coupling constant [5] and the integral is done over the hard layers, where both magnetizations are defined. The Landau–Lifshitz–Gilbert equation is then used to calculate the dynamics of the magnetizations.

The unidimensional model is a severe approximation for a description of the switching processes, where domain walls can form and play an important role, but for our investigation near the bending field the model should be quite accurate.

III. RESULTS

For the simulations, we use the Nmag micromagnetic simulation package [8], choosing the first-order finite element method (FEM) to discretize the space. The chosen mesh is a unidimensional lattice with constant spacing (FEM) to discretize the space. The chosen mesh is a unidimensional lattice with constant spacing (FEM) to discretize the space. The chosen mesh is a unidimensional lattice with constant spacing (FEM) to discretize the space. The chosen mesh is a unidimensional lattice with constant spacing (FEM) to discretize the space. The chosen mesh is a unidimensional lattice with constant spacing (FEM) to discretize the space. The chosen mesh is a unidimensional lattice with constant spacing (FEM) to discretize the space. The chosen mesh is a unidimensional lattice with constant spacing (FEM) to discretize the space. The chosen mesh is a unidimensional lattice with constant spacing (FEM) to discretize the space. The chosen mesh is a unidimensional lattice with constant spacing (FEM) to discretize the space. The chosen mesh is a unidimensional lattice with constant spacing}

The field $H_{Dy}$ is applied in the in-plane $x$-direction. The curve around the bending field is shown in the inset in more detail.

![Fig. 2. Hysteresis loop. The field is applied in the in-plane $x$-direction. The curve around the bending field is shown in the inset in more detail.](image)

![Fig. 3. Top: Trajectories of $(M)$ for $H_{app} = 3.60, 3.80, 4.00, 4.20$ T. At each step, the system reaches the equilibrium configuration for $H_{app} = H_{n}$ with a high damping parameter $\alpha = 0.5$ (dotted line). Then the field is changed to $H_{app} = H_{n} + \Delta H$ and $\alpha = 0.02$ is used to study the response (solid line) to the small increase in the field intensity. Bottom: $(M_x)$ is also plotted as a function of time for $H_{app} = 4.20$ T together with the fitted curve.](image)
because the magnetization of the hard layers is almost fixed for the considered range of the applied field. The alternating switching between the high and the low damping parameter can be distinguished clearly. The shape of these curves are all similar from one to the other: they are spirals compressed can be distinguished clearly. The shape of these curves are switching between the high and the low damping parameter produced as a reaction to the small perturbation $\Delta H$. Fig. 4 collects the results of the fits. The corresponding curves closely match the data. An example is shown in Fig. 3. The graphs in Fig. 4 clearly show that near the bending field the dynamical reaction of the system is amplified: the same perturbation $\Delta H$ produces wider oscillations with smaller frequency and which last longer (higher decay time $\lambda^{-1}$). The plot of the frequencies shows a minimum near $H_b$ and a qualitative behavior which is consistent with previous experimental and theoretical results [4]. The amplitudes, whose magnitude depends on the value chosen for $\Delta H$, show an interesting feature: the shapes of the spiral trajectories (Fig. 3) change with the applied field, being elongated in the in-plane $y$-direction for $H_{\text{app}} \ll H_b$ and in the out-of-plane the $z$-direction for $H_{\text{app}} \gg H_b$. We have repeated our studies increasing $\Delta H$ by a factor of 5 and decreasing it by a factor of 10. This does affect frequencies and decay times by less than 0.015% and 0.2%, respectively.

IV. Conclusion

We have carried out micromagnetic simulations of the dynamics of a tri-layer DyFe$_2$/YFe$_2$/DyFe$_2$ exchange spring system with realistic crystal field anisotropy near the bending field, showing how the magnetization reacts to small increments in the intensity of the applied field. We have shown that the dynamics of the components of the mean magnetization can be fitted with excellent results against the equation of motion of damped harmonic oscillators. We obtained the frequencies, the decay times, and the amplitudes of these oscillations and found that they have a minimum frequency, a maximum decay time, and a maximum amplitude near the bending field.

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References


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