

OPTIMAL DESIGN OF MONOMODE TRANSMITTER MODULE

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ABSTRACT

A simple model of an external cavity is used to investigate optimum configurations for achieving a high degree of spectral purity in one mode. A new figure of merit for monomode behaviour is defined.

INTRODUCTION

An attractive technique to achieve 1.55 $\mu\text{m}$  single-mode laser transmitters for high bit-rate long-haul optical communications systems is based on the use of a short external cavity. It has been shown<sup>(1)</sup> that a concave spherical mirror positioned about 200 $\mu\text{m}$  from one facet of the laser can produce sufficient feedback to give stable single longitudinal mode operation even under conditions of high-speed modulation. Control circuitry can be contained in a single integrated circuit which is designed to adjust the position of the external reflector so as to maximise the power emitted from the laser<sup>(2)</sup>.

In the present contribution we present an analysis of the mode selectivity offered by such a transmitter module and discuss the optimum configuration. The analysis is based on numerical solution of multimode rate equations under steady-state conditions.

ANALYSIS

The cavity configuration to be considered is illustrated in Fig. 1. A hemispherical mirror of reflectivity  $R_M$  is situated at distance  $L_e$  from one facet; the coupling of the laser to the external cavity is described by a field coupling coefficient  $\epsilon$ . The parameters  $R_M$  and  $\epsilon$  are conveniently combined into a single modified reflectivity  $R_E$  defined by  $R_E = \epsilon^2 R_M$ . The phase change in the cavity is given by  $\psi_e = 2\pi L_e / \lambda$  where  $\lambda$  is the wavelength. Standard theory then gives the effective reflectivity  $R$  of the laser facet plus external cavity as<sup>(3)</sup>

$$R = \frac{R_2 - 2\sqrt{R_2 R_E} \cos 2\psi_e + R_E}{1 - 2\sqrt{R_2 R_E} \cos 2\psi_e + R_2 R_E} \quad (1)$$

The modulation depth of this effective reflectivity is thus given by

$$R_{\max} - R_{\min} = \frac{4 \sqrt{R_2 R_E} (1-R_2)(1-R_E)}{(1-R_2 R_E)^2} \quad (2)$$

A plot of this quantity versus the external reflectivity  $R_E$  is given in Fig. 2 for various values of facet reflectivity  $R_2$ . For the usual case

achieved in practice<sup>(1,2)</sup> there is very weak external coupling ( $R_E < 1$ ) and then the maximum value of  $(R_{\max} - R_{\min})$  is obtained when  $R_2 = 1/3$ . Thus neither reflective nor antireflective coatings would increase the modulation depth of effective reflectivity, as also can be seen in Fig. 2. As long as the external coupling is small, uncoated lasers, when interacting with a cavity with no additional dispersive elements, are expected to be more selective than lasers with coated mirrors.

In order to analyse the behaviour of the laser in the external cavity, we have used the value for  $R$  from eqn. (1) in steady-state solutions of the multimode rate equations. The results are then expressed in terms of the photon densities  $N_m$  in each longitudinal mode  $m$ , taking  $m=0$  as the dominant mode. The procedure applied in the computer solution corresponds to the technique that would normally be adopted in practice, namely (i) tuning the gain spectrum above threshold so that the peak coincides with a free-running laser mode, and (ii) tuning the external cavity to make a maximum of  $R$  coincide with a laser mode. Since the rate equations contain no noise terms, the ratios  $N_0/N_m$  predicted by this method are usually much larger than those measured for real transmitters. In order therefore to produce results which could be meaningfully compared with experiment, we introduce a 'figure of merit',  $M_m$  for each mode  $m$ , defined as

$$M_m = \frac{(N_m/N_0)_{R_E}}{(N_{+1}/N_0)_{R_E=0}} \times 100\% \quad (3)$$

where the subscript  $R_E$  refers to the case with an external cavity and  $R_E=0$  refers to the free-running laser.

## RESULTS

Table 1a shows computed values of  $M_m$  for  $m = \pm 1, \pm 4$  and a range of values of  $R_E$ . The other parameters were  $L=200\mu\text{m}$ ,  $L_e \approx 200\mu\text{m}$ ,  $R_2=0.3$ , and other material parameters appropriate for  $1.55\mu\text{m}$  GaInAsP lasers<sup>(4)</sup> at twice threshold. For this case of  $L \approx L_e$ , since the group index of the laser material is approximately 4, the modulation of effective reflectivity given by the external cavity has a period equal to 4 mode spacings of the free-running laser. Using calculated gain spectra<sup>(4)</sup> appropriate to the drive current it is therefore possible for either the  $+4$  modes or the  $+1$  modes to compete for the 0 mode power, depending on the value of the reflectivity  $R_E$ . Thus Table 1a shows that for  $R_E=1\%$  and  $5\%$  the  $\pm 4$  modes are the strongest competitors whilst for smaller values of  $R_E$  (when tuned to the 0 mode) the  $+1$  modes are favoured.

When  $L_e \approx 400\mu\text{m}$  the maxima of effective reflectivity coincide with 0,  $+2$  mode wavelengths. This results in a higher power share for  $+2$  modes and a poorer mode selectivity (see Table 1b).

Table 1a also shows for  $R_E=0.1\%$  the effects of de-tuning the external cavity to coincide with modes on either side of the gain spectral maximum. This leads to asymmetry in the power spectrum, with the  $+4(-4)$  mode as a secondary mode when the external cavity is tuned to the longer-(shorter-) wavelength mode  $-1(+1)$  of the free-running laser.

For very low values of external reflectivity, the gain spectral variation will be as strong as that given by the external cavity reflectivity modulation. To investigate the values of reflectivity for which this may

occur we use eqn. (1) in conjunction with the usual laser threshold condition, to give

$$\sqrt{R_M} \approx \frac{\Gamma L \Delta g \sqrt{R_2}}{(1-R_2)(1+\cos 2\psi_e)} \quad (4)$$

where  $\Delta g$  is the gain difference between primary and secondary laser modes, and  $\Gamma$  is the optical confinement factor. For the parameters given above, eqn. (4) shows that  $R_E \approx 10^{-5}$  is the lowest value of external reflectivity for which the cavity mode selectivity dominates over that given by the internal gain spectrum.

### CONCLUSION

A simple model of an external cavity has been used with multimode rate equations in order to investigate the effects of varying reflectivity and tuning/detuning the cavity. The results are expressed in terms of a figure of merit which shows the degree of spectral purity as compared to that for the free-running laser. The optimum configuration for a  $1.55\mu\text{m}$  laser is  $L_e \approx L$  and uncoated laser facets. On the basis of the figure of merit the external hemispherical reflector should have a reflectivity of at least 0.1%

TABLE 1 Figure of merit  $M_m$  (note that smaller values of  $M_m$  correspond to a better selectivity).

1a.  $L_e \approx 200\mu\text{m}$

$R_E$ (%)	Tuned to laser mode	$M_m$ (%)			
		m			
		-4	-1	+1	+4
0	0	5.9	100	100	6.7
0.001	0	5.9	45	45	6.5
0.01	0	6.0	21	21	6.3
0.05	0	6.2	11	11	6.0
0.1	-1	3.7	6.4	9.5	13
0.1	0	6.4	8.0	7.9	5.8
0.1	+1	20	10	6.9	3.9
1	0	7.0	3.0	3.0	5.1
5	0	5.4	1.7	1.8	5.4

1b.  $L_e \approx 400\mu\text{m}$

		-2	-1	+1	+2
5	0	24	0.41	0.44	20

### ACKNOWLEDGEMENTS

BTRL are acknowledged for supporting this work. The authors thank M.R. Matthews for useful discussions. The paper is presented with the permission of the Director of BTRL.

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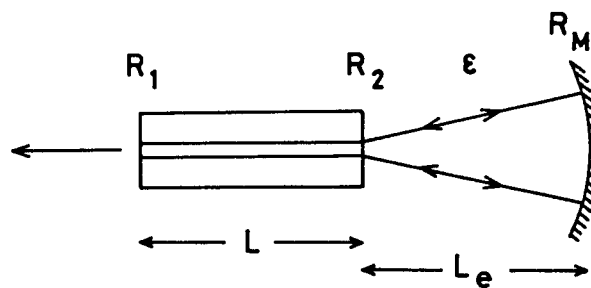


Fig. 1 External cavity configuration

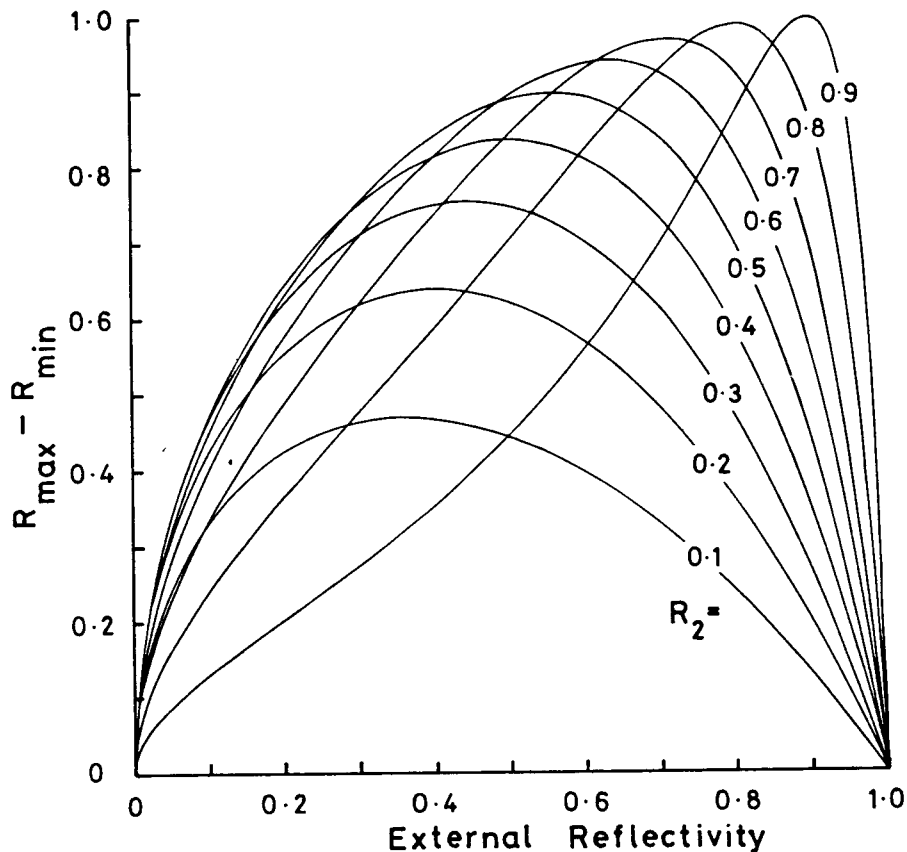


Fig. 2  $R_{\max} - R_{\min}$  vs  $R_E$  for  $R_2$  varying from 0.1 to 0.9